

## UNITS OF MEASUREMENT

- 1)  $v$  is measured in m/s, and  $a$  is measured in  $\text{m/s}^2$ .
- 2)  $F$  is measured in  $\text{N} = (\text{kg m}) / \text{s}^2$ .
- 3) and 4)  $k$  is measured in  $\text{J/m}^2$  or  $\text{N/m}$  or  $\text{kg/s}^2$  which all work out to the same thing.
- 5)  $E$  is measured in  $\text{N/C}$  which can also be written as  $(\text{kg m}) / (\text{C s}^2)$ .
- 6)  $k_e$  is measured in  $(\text{N m}^2) / \text{C}^2$  or  $(\text{kg m}^3) / (\text{C}^2 \text{s}^2)$ .
- 7)  $B$  is measured in  $\text{T} = (\text{N s}) / (\text{C m})$  or  $\text{kg} / (\text{C s})$ .
- 8)  $G$  is measured in  $(\text{N m}^2) / \text{kg}^2$  or  $\text{m}^3 / (\text{kg s}^2)$ .
- 9)  $I$  is measured in  $\text{A} = \text{C/s}$ .
- 10)  $V$  is measured in  $\text{V} = \text{J/C}$ .
- 11)  $R$  is measured in  $\Omega = \text{V/A}$  or  $(\text{J s}) / \text{C}^2$ .
- 12)  $\text{A} \bullet \text{V} = (\text{C/s}) \bullet (\text{J/C}) = \text{J/s}$ , also known as watts (W), the unit of measurement for power.
- 13)  $(1 \text{ g/cm}^3) \bullet (1 \text{ kg} / 1000 \text{ g}) \bullet (100 \text{ cm} / 1 \text{ m})^3 = 1000 \text{ kg/m}^3$ .

## DIMENSIONAL ANALYSIS

14)  $\text{N} \neq \text{kg/s}$ , so the formula doesn't work... but  $F = \frac{m \cdot v^2}{r}$  does work.

15)  $\text{m/s} \neq \text{m}^2/\text{s}^2$ , so the formula doesn't work... but  $v = \sqrt{\frac{F}{\left(\frac{\Delta m}{\Delta x}\right)}}$  does work.

16)  $\text{m}^3/\text{s} \neq 1/(\text{m s})$ , so the formula doesn't work... but  $\frac{\Delta \text{volume}}{\Delta t} = v \cdot \text{area}$  does work.

17) Units matching up does *not* guarantee that the formula is correct!  
 You can find a hilarious counterexample at <http://xkcd.com/687/>  
 However, if the units do *not* match up, that *does* tell you that something's wrong.

## SCIENTIFIC NOTATION

18)  $(5 \times 10^3 \text{ m}) \times (6.2 \times 10^4 \text{ m}^2) = 3.1 \times 10^8 \text{ m}^3$

19)  $(3 \times 10^4 \text{ m})^3 = 2.7 \times 10^{13} \text{ m}^3$

20)  $\frac{(2.4 \times 10^2 \text{ kg})}{(8 \times 10^{10} \text{ m}^3)} = 3 \times 10^{-9} \text{ kg/m}^3$

21)  $(4.18 \times 10^2 \text{ kJ}) + (7.9 \times 10^4 \text{ J}) = 4.97 \times 10^5 \text{ J}$  or  $4.97 \times 10^2 \text{ kJ}$

22) 
$$F_{\text{Sun on Earth}} = \frac{G \cdot m_{\text{Sun}} \cdot m_{\text{Earth}}}{r^2} = \frac{\left(6.67 \times 10^{-11} \frac{\text{m}^3}{\text{kg} \cdot \text{s}^2}\right) \cdot (1.99 \times 10^{30} \text{ kg}) \cdot (5.97 \times 10^{24} \text{ kg})}{(9.4 \times 10^8 \text{ km})^2}$$

$\approx 8.97 \times 10^{20} \text{ N}$  (note that km must be converted to m first!)